# Estimation of the Electric Field and Potential Distribution on Three Dimension Model of Polymeric Insulator Using Finite Element Method

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Abstract - This paper proposes Three Dimension Finite Element Model (FEM) to calculate the electric field and voltage distribution on outdoor polymeric insulator under clean and pollution conditions. The objective of this work is to comparison the effect of contamination and water droplets on potential and electric field distributions along the surface for two types of the insulator. Finite element method (FEM) is adopted for this work. The simulation results show that contaminations Cause more nonlinear potential distribution along the insulator surface while electric field distributions are obviously depended on contamination conditions. And also show that electric field distribution along straight sheds insulator higher than alternate shed insulator in case of surface contamination, and exist water droplets on the surface of the insulator.

Keywords - silicone rubber polymer insulator, electric field distribution, potential distribution, finite element method

#### I. INTRODUCTION

Polymer insulators, which have been used increasingly for outdoor applications, give better characteristics over porcelain and glass types: they have better contamination performance due to their surface hydrophobicity, lighter weight, possess higher impact strength, and so on. Polymer insulators are quite different from the conventional porcelain and glass insulators. [1-2]. Structure of a polymer insulator is shown in Fig. 1.

The basic design of a polymer insulator is as follows; a fiber reinforced plastic (FRP) core, attached with two metal fittings, is used as the load bearing structure. The presence of dirt and moisture in combination with electrical stress results in the occurrence of local discharges causing the material deterioration such as tracking and erosion.

In order to protect the FRP core from various environmental stresses, such as ultraviolet, acid, ozone etc., and to provide a leakage distance within a limited insulator length under contaminated and wet conditions, weather sheds are installed outside the FRP core.

Silicone rubber is mainly used for polymer insulators or composite insulators as housing material [3]

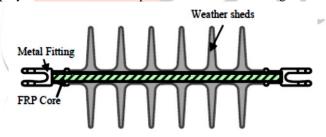


Fig. 1 Structure of a Polymer Insulator

However, since polymer insulators are made of organic materials, deterioration through ageing is unavoidable. Hence, ageing deterioration is a primary concern in the performance of polymer insulators. Artificial salt fog ageing tests have been most widely conducted on simple plates, rods, and small actual insulators for evaluating the anti-tracking and/or anti-erosion performance of housing materials for polymer insulators. [4-5]

Many of the research in this work were provided analysis on the two-dimensional model, but this paper presents a new Three-dimensional model, incorporates the real Insulator geometrical dimensions, and its material properties.

Two types of silicone rubber insulator are used: straight sheds with leakage distance 290 mm and alternate shed with leakage distance 290 mm Fig.2. The 15 kV polymeric insulator models are simulated under clean, polluted surface conditions using (FEM) Electrostatic Software.

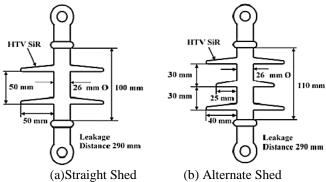


Fig. 2 Dimensions of Different Types of SIR Insulator.

#### II. FINITE ELEMENT METHOD

There are several methods for solving partial differential equation such as Laplace's and Poisson equation. The most widely used methods are Finite Difference Method (FDM), Finite Element Method (FEM), Boundary Element Method (BEM) and Charge Simulation Method (CSM). In contrast to other methods, the Finite Element Method (FEM) takes into accounts for the nonhomogeneity of the solution region. Also, the systematic generality of the methods makes it a versatile tool for a wide range of problems.

The underlying premise of the method states that a complicated domain can be sub-divided into series of smaller regions in which the differential equations are approximately solved. By assembling the set of equations for each region, the behavior over the entire problem domain determined. Other words, using the Finite Element Method (FEM), the solution domain is discretized into smaller regions called elements, and the solution is determined in terms of discrete values of some primary field variables \_ (e.g. displacements in x, y & z directions) at the nodes.

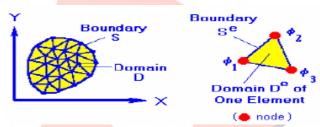


Fig. 3. Typical finite element subdivisions of an irregular domain and typical triangular element.

The number of unknown primary field variables at a node is the degree of freedom at that node. For example, the discretized domain comprised of triangular shaped elements is shown in Fig. 3. In this example each node has one degree of freedom. [1-6]

## III. PROBLEM SOLUTION EQUATION

Electric field and potential distributions calculation

One simple way for electric field calculation is to calculate electric potential distribution. Then, electric field distribution is directly obtained by minus gradient of electric potential distribution. In electrostatic field problem, [7]

To illustrate the process, the method will be applied to the modelling of an electrostatic field. The partial differential equation that describes the voltage potential distribution within any given region is derived as follows: [8]

$$\nabla \cdot \mathbf{D} = \boldsymbol{\rho}_{\boldsymbol{v}} \tag{1}$$

Where **D** is electrical flux density,  $C.m^{-2}$ ,  $\rho v$  is free charge density,  $C.m^{-3}$ , and since

 $\mathbf{D} = \boldsymbol{\varepsilon}_0 \boldsymbol{\varepsilon}_r \mathbf{E}$  then Equation (1) becomes:

$$\nabla(\varepsilon_0 \varepsilon_r E) = \rho_v \tag{2}$$

 $\nabla(\varepsilon_{\theta}\varepsilon_{r}E) = \rho_{\nu} \tag{2}$  Where E is electrical stress,  $\mathrm{Vm}^{-1}$ ,  $\varepsilon_{\theta}$  is  $8.85419 \times 10^{-12}$ ,  $\mathrm{Fm}^{-1}$  and  $\varepsilon_{r}$  is relative permittivity.

To formulate in terms of the voltage potential, V can be written in terms of E:

$$-\nabla V = E \tag{3}$$

Substituting this in Equation (2) results in the following equation:

$$\nabla \cdot \{ \varepsilon_0 \varepsilon_r (-\nabla V) \} = \rho_{\nu} \tag{4}$$

Equation (4) can be rewritten for a homogeneous region as:

$$\nabla . \nabla V = -\frac{\rho_v}{\varepsilon_0 \, \varepsilon_r} \tag{5}$$

Equation (5) is called Poisson's equation and applies to a homogeneous medium.

If  $\rho v$  is zero the equation reduces to Laplace's equation for homogeneous media. This is shown in full by Equation (6) (an expansion of Equation (5) in Cartesian coordinates):

$$\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2} = \mathbf{0} \tag{6}$$

Equation (6) is the partial differential equation that describes the voltage potential distribution in high voltage situations where the medium is homogeneous and the charge density is zero. If the medium is non-homogeneous then Equation (6) is written as:

$$\varepsilon_0 \varepsilon_r \left( \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2} \right) = \mathbf{0} \tag{7}$$

For each region. This is to allow for the different permittivities in the different regions.

To use Equation (7) in a finite-element formulation requires the equation to be transformed into an energy functional form that relates directly to the electrical energy of the system. [8]

## B. The energy functional illustrated

The total electrical energy in a system of volume  $\Omega$  may be written as:

$$F = \frac{1}{2} \int_{\Omega} D \cdot E d\Omega \tag{8}$$

i.e.

$$F = \int_{\Omega} \frac{1}{2} \varepsilon_0 \varepsilon_r E^2 d\Omega \tag{9}$$

If it is assumed that the permittivity is constant within the region concerned, then Equation (9) may be used to write the energy (in a Cartesian coordinate system) as:

$$F = \int_{\Omega} \frac{\varepsilon_0 \varepsilon_r}{2} \left[ \left( \frac{\partial V}{\partial x} \right)^2 + \left( \frac{\partial V}{\partial y} \right)^2 + \left( \frac{\partial V}{\partial y} \right)^2 \right] dx dy dz$$
 (10)

It can be shown that this is the functional that, when differentiated with respect to V and equated to zero, gives a distribution of V that satisfies the governing partial differential equation. Physically, the process corresponds to minimizing the stored electrical energy i.e. the potential energy of the system for the imposed boundary conditions. The differentiation is most conveniently carried out on the discretized system.

For element e

$$F_{e} = \frac{\varepsilon_{0}\varepsilon_{r}}{2} \int_{e} \left[ \left( \frac{\partial V}{\partial x} \right)^{2} + \left( \frac{\partial V}{\partial y} \right)^{2} + \left( \frac{\partial V}{\partial y} \right)^{2} \right] dx dy dz$$
 (11)

Where suffix e indicates integration over an element. Hence, the contribution to the rate of change of F with V from the variation of potential of node i in element e only,  $\chi_e$ , is:

$$x_{e} = \frac{\partial F_{e}}{\partial V_{i}} = \frac{\varepsilon_{0}\varepsilon_{r}}{2} \int_{e} \frac{\partial}{\partial V_{i}} \left[ \left( \frac{\partial V}{\partial x} \right)^{2} + \left( \frac{\partial V}{\partial y} \right)^{2} + \left( \frac{\partial V}{\partial y} \right)^{2} \right] dx dy$$
(12)

$$x_{e} = \frac{\varepsilon_{0}\varepsilon_{r}}{2} \int_{e} \left[ 2\frac{\partial V}{\partial x} \cdot \frac{\partial}{\partial V_{i}} \left( \frac{\partial V}{\partial x} \right) \right] dx dy dz$$

$$+ 2\frac{\partial V}{\partial y} \cdot \frac{\partial}{\partial V_{i}} \left( \frac{\partial V}{\partial y} \right) dx dy dz$$

$$+ 2\frac{\partial V}{\partial z} \cdot \frac{\partial}{\partial V_{i}} \left( \frac{\partial V}{\partial z} \right) dz dy dz$$

$$(13)$$

### C. Numerical representation

To solve high voltage problems using the finite-element method requires Equation (13) to be equated to zero. To represent the problem numerically, the problem region is divided into elements and Equation (13) is applied at the nodes forming the element vertices. The variation of the potential over the elemental shape has then to be approximated by a polynomial distribution (known as the shape function). The order of the chosen polynomial will dictate the type of element used, for example a linear distribution would only require a simple triangular element. For higher order shape functions, the number of nodes describing the element

must be capable of defining the order used, e.g. a quadratic shape function over a triangular element requires nodes at the middle of each element side. [8]

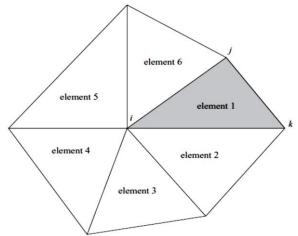


Fig.4. Elements associated with node i.

There will be contributions to the rate of change of the region functional  $\chi$  with respect to the potential  $V_i$  at node i from all the elements connected to i. In the case shown in Figure 4, there will be contributions from elements 1 to 6. Hence, generally, the contribution to  $\partial F/\partial V$  from a change in  $V_i$  is:

$$\frac{\partial F}{\partial V_i} = \sum_{e} \frac{\partial F_e}{\partial V_i} \tag{14}$$

Where  $\sum_{\mathbf{e}}$  represents the summation of contributions from all elements associated with  $V_{i}$  i.e., all the elements connected to node i.

When these derivatives are equated to zero, a group of simultaneous equations is formed. These can be written in matrix form as:

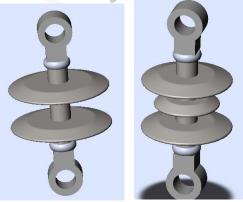
$$\left[S_{t}\right]\left\{V_{i}\right\} = 0\tag{15}$$

Where [St] is a square matrix known as the stiffness matrix and is formed from the geometric coordinates of the nodes defining the elements and the material properties.

*Vi* is a column matrix containing all the nodal potentials. The coefficient stiffness matrix will be sparse, i.e. it will contain many zeros since, from the discussion above,

# IV. FEM MODEL FOR TWO TYPES POLYMERIC INSULATOR

Two models of polymer insulator, "Straight Shed and Alternate Shed" was selected to simulate electric field and potential distributions in this study. The basic three dimensions design of a polymer insulator is as follows; a fiber reinforced plastic (FRP) core having relative dielectric constant of 7.1, attached with two metal fittings, is used as the load bearing structure. Weather sheds made of high temperature vulcanized silicone rubber (HTV SiR) having relative dielectric constant of 4.3 are installed outside the FRP core. Surrounding of the insulator is air having relative dielectric constant 1.0. A 15 kV voltage source directly applies to the lower electrode while the upper electrode connected to ground. [9]. Three dimensions models of the two type polymer insulators for FEM analysis are shown in fig (5).



(a)Straight Shed (b) Alternate Shed Fig. 5 Three dimension models of the two type polymer insulators for FEM analysis.

This paper investigates the Electric field, and voltage distribution of the 15 kV polymeric insulators at two different surface conditions such as:

Case 1: Dry and clean insulator.

Case 2: Non-uniform pollution layer, and Water droplets on the insulator surface.

Properties	SI R	FR P cor e	Pollutio n layer	Water drople t	Ai r
Relative Permittivity ε	4.3	7.1	8	81	1
Conductivity, µs/cm	0	0	100	500	0
Thickness/Hei ght	-	ı	100µm	2mm	-

Table 1. Material properties of FEM model

Tab. 1 shows the properties of the materials such as relative permittivity, conductivity and thickness/ height of pollution layer and water droplets used for the FEM modeling of the insulators. The insulator is equipped with metal fittings at both line and ground ends. [10]

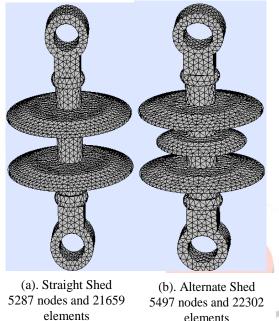


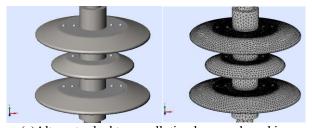
Fig. 6 Finite element Mesh results.

The whole problem three-dimensional models in Fig. 5, and Air box surrounding is fictitiously divided into small triangular areas called domain. The potential, which is unknown throughout the problem domain, is approximated in each of these elements in terms of the potential in their vertices called nodes. The most common form of approximation solution for the voltage within an element is a polynomial approximation.

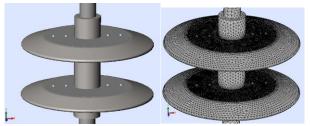
The obtaining surface Mesh results are 5,287 nodes and 21,659 elements for straight sheds type insulator and 5,497 nodes and 22,302 elements for alternate sheds type insulator, respectively. The obtaining results are shown in Fig. 6.

# V. RESULTS AND DISCUSSIONS

Clean and contamination conditions are simulated in this study. In case of contamination condition water droplets and non-uniform pollution layer are placed on the two type insulator surfaces as shown in Fig.7.

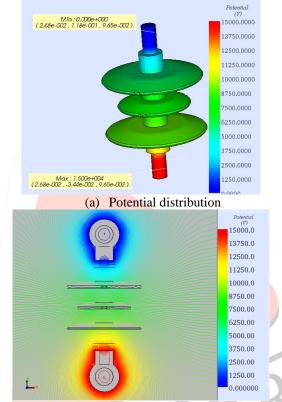


(a)Alternate shed type pollution layer and meshing

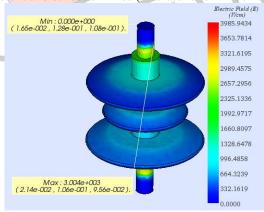


(b)Straight shed type pollution layer and meshing Fig.7. Pollution layer and meshing for two type insulator

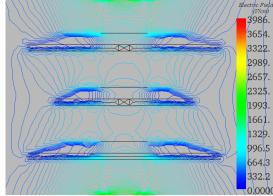
Potential and electric field distribution results for Alternate Sheds type under dry and clean conditions are shown in Fig. 8.



(b) Potential distribution lines (Insulator and Air box surrounding)



(c) Electric Field Distribution



(d) Electric Field Distribution lines (Insulator and Air box surrounding)
Fig. 8 Alternate Sheds Insulator Potential and Electrical field Distribution under Clean Condition.

Also electrical field along leakage distance of the insulator under dry and clean conditions are shown in Fig. 9.

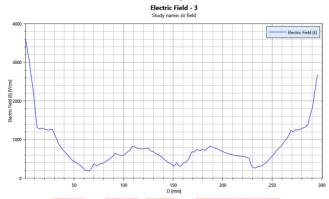
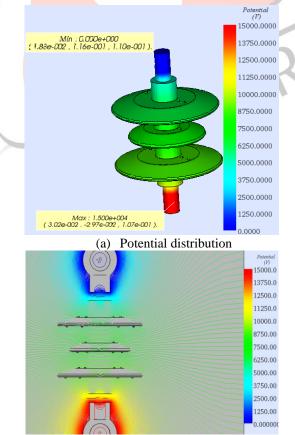
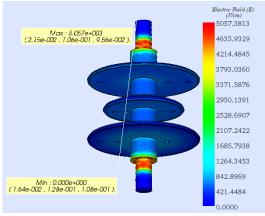


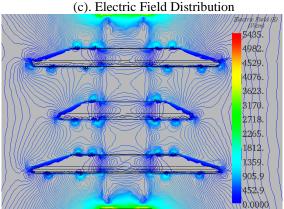
Fig. 9 Electrical field along leakage distance for Alternate Sheds Insulator under Clean Condition.

The potential and electric field distribution under pollution condition for the alternate shed type are illustrated in Fig.10.



(b) Potential distribution lines (Insulator and Air box surrounding)





(d) Electric Field Distribution lines (Insulator and Air box surrounding)
Fig. 10 Alternate Sheds Insulator Potential and Electrical field Distribution under Pollution Condition.

The electrical field along leakage distance of the insulator under contamination conditions illustrated in Fig.11

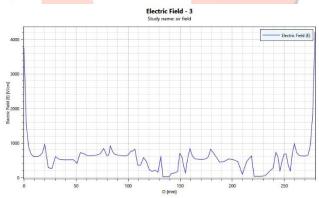
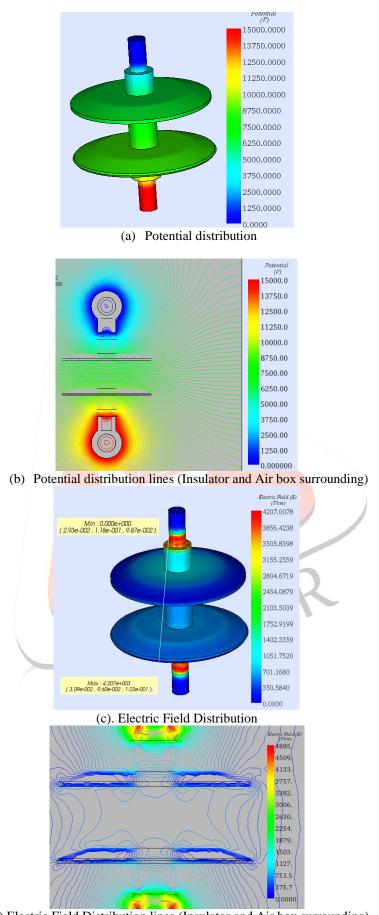


Fig. 11 Electrical field along leakage distance for Alternate Sheds Insulator under Pollution Condition.

As the same potential distribution and electric field distribution results for Straight Sheds type under dry and clean conditions are shown in Fig. 12.



(d) Electric Field Distribution lines (Insulator and Air box surrounding)
Fig. 12 Straight Sheds Insulator Potential and Electrical Field Distribution under Clean Condition.

The electrical field along leakage distance of the insulator under dry and clean conditions are shown in Fig. 13.

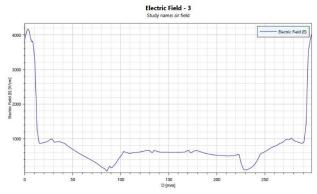
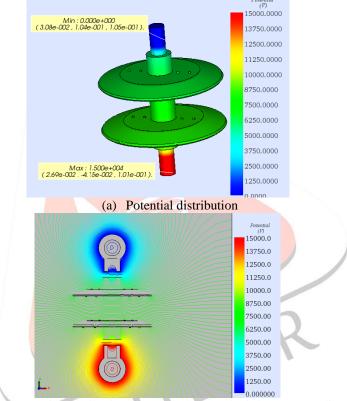
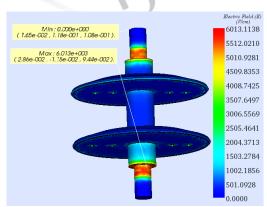


Fig. 13 Electrical field along leakage distance for Straight Sheds Insulator under Clean Condition.

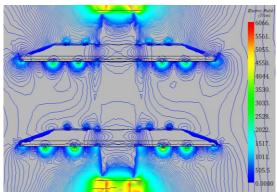
The potential and electric field distribution under pollution condition for the straight shed type are illustrated in Fig.14.



(b) Potential distribution lines (Insulator and Air box surrounding)



(c). Electric Field Distribution



(d) Electric Field Distribution lines (Insulator and Air box surrounding)

Fig. 14 Straight Sheds Insulator Potential and Electrical Field Distribution under Pollution Condition.

The electrical field along leakage distance of the insulator illustrated in Fig.15

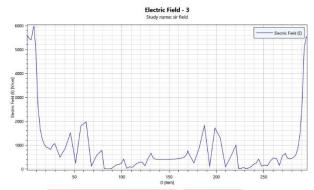


Fig. 15 Electrical field along leakage distance for Straight Sheds Insulator under Pollution Condition.

Comparison results illustrated in Fig.9 and Fig.11, are shown that obvious difference in magnitude of electric field and nonlinearity can be seen on the sheds of the alternate sheds insulator in case of contamination.

As the same, in the results illustrated in Fig.13 and Fig.15, shown that obvious difference in magnitude of electric field and nonlinearity can be seen on the sheds of the straight sheds insulator in case of contamination.

In case of dry and clean conditions, comparison results illustrated in Fig.8 and Fig.12 shown that the electric field intensity on Straight Sheds type (with maximum value

4207(V/cm)), is Higher than the electric field intensity on Alternate Sheds type (with maximum value 3986(V/cm)).

In case of contamination with water droplets conditions, comparison results illustrated in Fig.10 and Fig.14 shown that the electric field intensity on Straight Sheds type (with maximum value 6066(V/cm)), is Higher than the electric field intensity on Alternate Sheds type (with maximum value 5057(V/cm)).

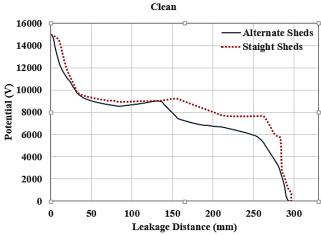


Fig. 16 Comparison of Potential Distribution for two type insulator under clean condition

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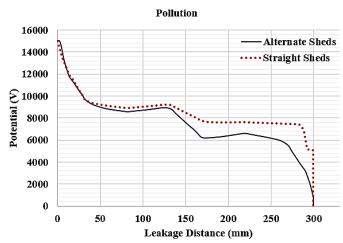


Fig. 17 Comparison of Potential Distribution for two type insulator under Pollution condition.

Comparison of potential distribution along leakage distance under clean and contamination condition for two type insulator is illustrated in Fig.16 and Fig.17 respectively show that more nonlinear potential distribution obtained from the straight sheds insulator comparing with the alternate sheds type.

#### VI. CONCLUSION

In many research, the potential and electric field distribution on high voltage polymer insulators has been estimated in two-dimension models, but in this paper, a three-dimensional model used to study the same Insulators, and this gives a high accuracy of the study results. The electric field and potential distributions on Straight sheds & Alternate shed silicone rubber polymer insulators under clean and contamination conditions were investigated by using FEM. Higher magnitude of electric field distribution and more nonlinear potential distributions on the straight sheds insulator comparing with the alternate shed type obtained from the simulation results by using Finite Element Method. And it's caused more electric discharge on the insulator surface. More discharge activities caused severe surface damages and possible flashover within operating conditions.

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